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## Ultralow lattice thermal conductivity at room temperature in $\text{Cu}_4\text{TiSe}_4$

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### Abstract:

Ultralow thermal conductivity draws great attention in a variety of fields of applications such as thermoelectrics, thermal barrier coating, etc. Herein, crystal structure and transport properties of  $\text{Cu}_4\text{TiSe}_4$  is reported.  $\text{Cu}_4\text{TiSe}_4$  is a unique example of a non-toxic and low-cost material that exhibits lattice ultra-low thermal conductivity of  $0.19 \text{ W m}^{-1}\text{K}^{-1}$  at room temperature. The main contribution to the unusually low thermal conductivity is connected with the atomic lattice and its dynamics. This ultralow value of lattice thermal conductivity ( $k_L$ ) can be attributed to the presence of the localized modes of Cu which partially hybridized with the Se atoms, which in turn leads to avoid crossing of acoustic phonon modes that reaches the zone boundary with a reduced frequency. Like a phonon glass electron crystal,  $\text{Cu}_4\text{TiSe}_4$  could also open the route for the finding of efficient thermoelectric materials, even, with chalcogenides of relatively high electrical resistivity and a large band gap, providing that their structures offer a sublattice with lightly bound cations.

**Introduction:**

In every energy conversion processes, certain percentage of heat is always liberated as universal by-product and mechanical work is one of the major source of energy dissipation. The unutilized heat waste could be effectively minimised by using thermal barrier coatings and refractories [1] or could be converted to electrical energy with the aid of efficient thermoelectric materials [2-5]. Therefore, continued search for new crystalline solid materials that can deliberately block the transportation of heat by virtue of their ultralow thermal conductivity ( $k$ ) is underway.

Phonons and free charges are the routine carriers of heat in crystalline solids except in lead halide perovskites[6], where the photo generated hot charge carriers intrinsically inhibit the phonon propagation during cooling. The leading contribution to the thermal conductivity is generally connected with the atomic lattice and its dynamics. The lattice thermal conductivity ( $k_L$ ) is formulated as  $k_L = 1/3C_v v l$  within the frame work of kinetic theory, where  $C_v$ ,  $v$  and  $l$  represent the specific heat at constant volume, group velocity of phonon and the phonon mean free path, respectively. In general, reduced  $k_L$  is achieved by two ways. Materials can be modified extrinsically by introducing point defect by incorporating foreign elements at the interstitial or lattice sites though the formation of solid solution. Another way is the modification of structural parameters (e.g; strains) intrinsically by altering the particles size which is directly related to lattice dynamics. All these strategies reduce the phonon relaxation time and hinder heat flow.

The compounds like clathrates [7] and skutterudites [8] could hold guest atoms into the cage-like structural voids, which substantially lower the  $k_L$  with low frequency rattling-like motion of the guest atoms. In the “phonon glass-electron crystal (PGEC)” compounds such as  $\text{Cu}_2\text{Se}$ [9],

Cu<sub>3</sub>SbSe<sub>3</sub>[10], AgCrSe<sub>2</sub>[11], and AgCuX (X = S, Se, and Te) [12], liquid-like movement of cations also causes lowering of  $k_L$ .

Cu-based chalcogenides materials (in bulk) have been extensively investigated for the application of thermoelectric [13–24] and photo-voltaic [25–29] over the past few years. High natural abundance, low cost of Cu and chalcogens (e.g. S, Se) and suitable band gaps have made them very attractive candidates for photovoltaic applications.

Considering the importance of low-cost, high-performance materials for sustainable energy applications, the investigations are pursued in the copper-metal-chalcogenides (CMC) system. In this research program, Cu-Ti-Ch (Ch = Chalcogen) ternary system is the subject of our investigation. A literature survey reveals that the Cu<sub>4</sub>TiS<sub>4</sub> and Cu<sub>2</sub>TiTe<sub>3</sub> were structurally studied by Klepp *et al.*[30] and Keane *et al.*[31]. But there was no Se based compound reported in the ternary Ti-Cu-Se system when the investigation was initiated. In the recent past, a report describing the existence of Cu<sub>4</sub>TiSe<sub>4</sub> has been published, which is focused on the crystal structure of the compound and has revealed its potential as a promising light-absorber in solar cells application. According to the report, the room temperature structure of Cu<sub>4</sub>TiSe<sub>4</sub> (Table S1) was solved in a centrosymmetric space group  $F\bar{4}3c(219)$  with a lattice constant,  $a = 11.2936(2) \text{ \AA}$  [32]. The structure contains 72 atoms per cell and has been reported as a  $(2a)^3$  – superstructure of sylvanite (Cu<sub>3</sub>MS<sub>4</sub>, M=V, Nb, Ta).

The current investigation includes the synthesis, crystal structure and transport properties of Cu<sub>4</sub>TiSe<sub>4</sub>. The ternary compound has been synthesized from the highly pure constituent elements by high-temperature solid-state synthesis. The crystal structure has been studied by means of single-crystal X-ray diffractometry and energy dispersive X-ray diffraction analysis (EDX). The

structure model in this investigation differs from the previously reported model by Erica M. Chen *et al.* Our investigation shows that the structure adopts,  $\text{Cu}_3\text{VS}_4$  ( $\bar{P}43m$ ;  $cP8$ ,  $a=5.39(1)$  Å), instead of its superlattice. The thermal conductivity of disordered  $\text{Cu}_4\text{TiSe}_4$  is found to be as small as  $0.19 \text{ W m}^{-1} \text{ K}^{-1}$ , a factor of 12 smaller than the thermal conductivity of  $\text{CuSe}$  and factor of 3 smaller than  $\text{Cu}_2\text{Se}$  at room temperature. This is probably the first ternary compound among CMC [33-38] and binary copper-chalcogenide with the lowest thermal conductivity at room temperature. Both experiment and computer simulation were employed to understand the ultralow thermal conductivity in this crystalline solid.

## Experimental Section:

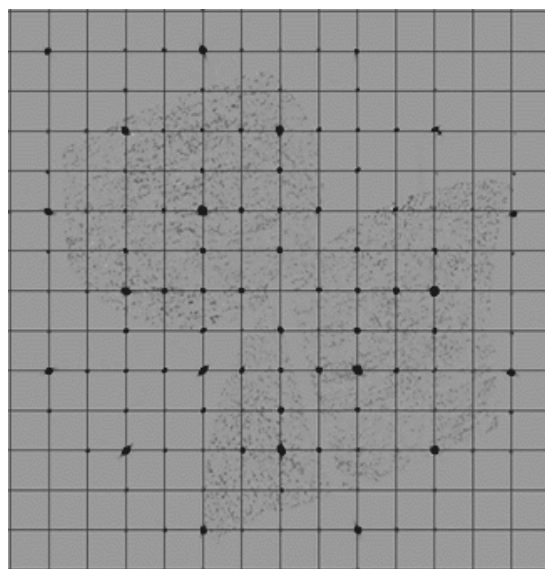
### Synthesis.

The samples were prepared by high-temperature solid-state synthesis from highly pure constituent elements (Ti powder, 99.99%; Cu ingot, 99.99%; Se powder, 99.999%). Initially elemental Ti, Cu, and Se were taken approximately in the ratio of 1:2:3 in a quartz tube and the tube was sealed under vacuum (about  $10^{-5}$  mbar). The ampoule was heated at a temperature of  $900^\circ\text{C}$  with a rate of  $180^\circ\text{C}/\text{hour}$ , annealed at this temperature for 120 hours and then slowly cooled down to  $300^\circ\text{C}$  over a period of the 96 hours and then allowed to cool to room temperature. The black coloured crystals were obtained from the crushed ingot. The crystals were mechanically separated, were analysed compositionally by Energy Dispersive X-ray Spectroscopic (EDX) technique and it showed the approximate composition of  $\text{Cu}_4\text{TiSe}_4$ . Subsequently, a series of samples were synthesised according to the EDX composition. To improve the quality of single crystal for structural characterisation, the samples were further annealed at  $900^\circ\text{C}$  for the period of 100 hours

and finally cooled down to 200°C at a rate of 6°C/hour. However, phase pure polycrystalline samples were prepared following the temperature program used by Erica M. Chen *et al.*[32].

### Single Crystal X-ray diffraction data collection and processing.

The single crystals (C1, C2, and C3) were mechanically separated from the crushed ingot and picked on a glass slide. The cuboid crystals of approx. dimensions ~0.2 mm were picked on the tip of the glass fibre by tiny amount of glue and mounted on goniometer head. The diffraction intensities were collected on BRUKER D8 VENTURE with PHOTON II detector equipped with graphite-monochromatic Mo-target  $K\alpha$  radiation ( $\lambda = 0.71073 \text{ \AA}$ ) at ambient temperature. Data collection, reciprocal space construction, and data reduction were performed Apex III software and CrysAlis Pro. The structure solution and the structure refinement were carried out using the *Jana2006* program [39-40]. The reflections were indexed on the basis of a ~5.6 Å primitive cubic unit cell [Fig. 1] for the room temperature dataset.



**Fig.1.** A reciprocal space view ( $hk0$ ) of a cubic unit cell with a lattice parameter of  $a=5.6458(1)$  Å. Single lattice is clearly visible (black) without any superstructure reflection.

It is worth mentioning that the diffraction data collected on  $\text{Cu}_4\text{TiSe}_4$  were thoroughly checked, and there is absolutely zero indication of Bragg reflections in  $(hk\frac{1}{2})$  and  $(hk\frac{3}{2})$ , which suggest there is no cell doubling, or otherwise any diffuse scattering (supporting information Fig. S1).

#### **Powder X-ray diffraction data collection.**

To confirm the purity, analyse the adjacent phases, and to identify new phases, X-ray powder diffraction experiments were performed for all the synthesised samples. Ingots were crushed and thoroughly ground into powder with agate mortar and pestle. Powder X-ray diffraction data were collected at room temperature by using BRUKER D2 PHASER diffractometer with  $\text{Cu-K}\alpha$  X-ray radiation ( $\lambda=1.5418\text{\AA}$ ). Data measurement was carried out with a step size of  $0.02^\circ$ . The powder diffraction data of the prepared samples were analysed by Rietveld refinement using *Jana2006* program.

#### **Field emission scanning electron microscopy (FE-SEM) and energy dispersive X-ray spectroscopic analysis (EDX).**

Black coloured selected crystals from the crushed ingot were subjected for chemical analysis in a Nova Nano SEM 450 field emission scanning electron microscope (FE-SEM) equipped with Bruker energy dispersive X-ray analyser (EDX). EDX data were acquired with an accelerating voltage of 10-15 kV and an accumulation time of the 50s.

**Pallet Preparation.**

A pallet was made from a phase pure finely powdered sample under a pressure of 50 MPa at 573K by Spark Plasma Sintering (SPS) technique. Sample was sintered at this temperature and pressure for 10 minutes.

**Physical property measurement.**

Thermal conductivity, electrical resistivity and heat capacity were measured in Quantum Design PPMS at low temperature. Diffuse reflectance spectroscopic measurement was carried out in a Varian Cary 5000UV-Vis-NIR spectrometer in the wavelength ranging 200nm to 2000nm.

**Computational details:**

The first principle calculations were carried out to analyze the electronic structure and transport properties of  $\text{Cu}_4\text{TiSe}_4$  within the framework of density functional theory (DFT) [41-42]. The calculations were performed using Vienna ab-initio simulation package (VASP) [43], which is a plane wave based electronic structure code. The Generalized Gradient Approximation (GGA) [44] with Perdew-Burke-Ernzerhof (PBE) formulation was used to treat the electronic exchange and correlation. A plane-wave cutoff energy of 550 eV and an energy convergence criterion of  $10^{-4}$  eV were used. Convergence in energy was checked with respect to K-mesh size and a  $15 \times 15 \times 15$  K-mesh was employed for the conventional cell with nine atoms. In all cases, ionic as well as geometric relaxations were performed.

The phonon band structure was calculated using the finite displacement method as implemented in the phonopy [45] code. Converged supercell of  $2 \times 2 \times 2$  was used to calculate the phonon band structure. The amplitude of the displacements was fixed to  $0.01 \text{ \AA}$ , and the forces were converged

to the accuracy of  $10^{-8}$  eV/Å. The phonon group velocity  $v$  ( $v = \frac{d\omega}{dk}$ ), mode resolved phonon group velocity  $v_i$  ( $v_i = \frac{d\omega_i}{dk}$ ), Grüneisen parameter  $\gamma$  ( $\gamma = \frac{-V_0}{\omega} \frac{d\omega}{dV}$ ), and mode resolved Grüneisen parameter  $\gamma_i$  ( $\gamma_i = \frac{-V_0}{\omega_i} \frac{d\omega_i}{dV}$ ) were extracted from the harmonic phonon band dispersion using self-written python based extensions to phonopy-VASP. For calculating the  $\gamma$  and  $\gamma_i$ , the lattice was subjected to biaxial strains of  $\pm 2$  %. Finally, the Asen-Palmer modified version of the Debye Callaway theory parametrized for solid [46] was used to calculate lattice thermal conductivity ( $k_L$ ) of the compounds (which is provided in the supplementary material).

## Result and discussions:

### Structure solution, refinement and phase analysis.

The structure solution were carried out by *Superflip* [39], which is implemented with *Jana2006*. Structural refinements were performed in *Jana2006* software package [40]. *Superflip* is used only to create the original model whilst *Jana2006* is used for the refinement. The refinement is a standard least squares refinement of the positions and displacement parameters of the atoms. The structure solution of C1 yielded three crystallographically independent sites in the unit cell, out of them, one is selenium site (Se1; 4e), one is titanium site (Ti1; 1b) and another one is Cu site (Cu1; 3c). At this stage, the preliminary structure refinement converged at R(F) of 11%. An additional atomic position (4e) at  $x \approx 0.83$  and  $y = z \approx 0.17$  was identified in residual electron density maps and included as copper (Cu2). The structural model was refined. Cu2 site showed relatively large atomic displacement parameter. Hence, this particular site was checked for partial occupancy, and subsequent refinement resulted in the residual value of 10%. An additional site (1a) at (0, 0, 0) was further identified in residual electron density map and assigned as copper (Cu3). The distance

between Cu2 site and Cu3 was too short ( $\sim 1.52 \text{ \AA}$ ). Hence, Cu3 site was checked for partial occupancy. The structural model was refined and subsequent refinement resulted in the residual value of  $\sim 8\%$ . Cu2 and Cu3 split into five positions [one at (0, 0, 0) and four at  $4e; x \approx 0.83, y = z \approx 0.17$ ]. At (0, 0, 0) site occupancy factor (SOF) of Cu is  $\sim 0.34$  and SOF of Cu at each 4e site is  $\sim 0.16$ . The correlation between the independently refined occupations factors kept the total occupancy of disordered Cu sites ( $4 \times \text{SOF}(\text{Cu}_2) + \text{SOF}(\text{Cu}_3)$ ) close to unity [**Fig. 2**]. It is worthy to mention that positional disorder in copper site was previously found in copper-based chalcogenides (e.g.  $\text{Cu}_4\text{MS}_4$  (M= Ge, Sn)) [**47**]. Harmonic ADPs of the atoms were taken into account for all including the positionally disordered sites.

This model was used as a starting model for the refinement of single-crystal X-ray diffraction data collected for compound C2 and C3. The final refinement including an isotopic extinction correction yielded  $R(F^2)$  ( $F^2 > 3\sigma(F^2)$ ) values between 3% and 4% [**Table S2**]. Measurement details and refinement results are mentioned in **Table S2**. The atomic coordinates together with their site occupancy and thermal displacement parameters are listed in **Table S3**.

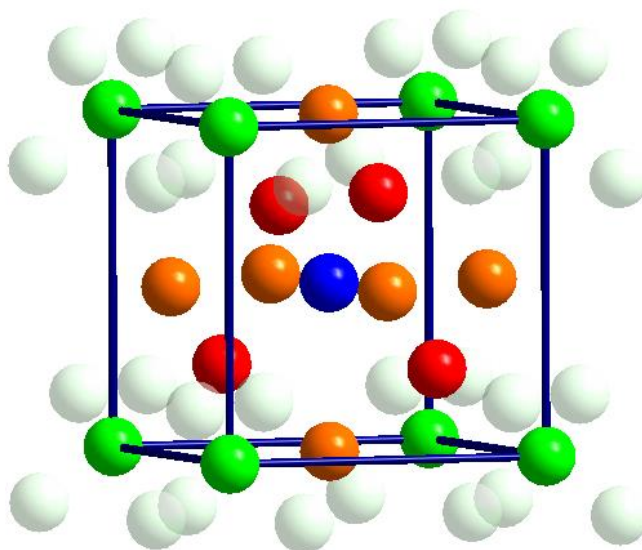
SCXRD data refinement gave a composition close to that of composition received from EDX analysis [**Table S2**]. For physical property measurement, the phase pure samples were prepared by using the temperature program according to previous report by Erica M. Chen *et al.* [**Fig. S2**]. Phase analysis was performed with different loaded composition [**Table S3**] and no phase-width was observed for our reported compound( supporting information **Table S4**).

It is worth to mention that Erica M. Chen *et al.* [**Fig. S3**] have used a larger unit cell with a lattice constant,  $a = 11.2936(2) \text{ \AA}$  to describe the structure of  $\text{Cu}_4\text{TiSe}_4$ . The structural model, which was refined in the space group  $F\bar{4}3c$  (219), contains 72 atoms. The atoms are distributed only at high

symmetry sites (32e, 24d, 8a and 8b), and, in standard settings, it must be described by the space group  $P\bar{4}3m$  with the unit cell parameter  $a=5.6468 \text{ \AA}$ , the same as what we find for our structure (Supporting information Fig. S3, SI1). Thus, it is concluded that the reported crystal structure by *Chen et al.* was incorrect. Moreover, the large atomic displacement parameters in a position  $(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$  suggests that they have erroneously assigned Ti atom (Table S0) in their proposed structural model.

### Crystal Structure.

The crystal structure of  $\text{Cu}_4\text{TiSe}_4$  is closely related to mineral sylvanite,  $\text{Cu}_3\text{VS}_4$  ( $P\bar{4}3m$ ;  $cP8$ ,  $a=5.39(1) \text{ \AA}$ ) [33] and  $\text{Cu}_4\text{TiS}_4$  ( $tI18$ ;  $I\bar{4}2m$  (121),  $a = 5.448(1) \text{ \AA}$   $c = 10.565(2) \text{ \AA}$ ) [Fig S4] [30].



**Fig. 2.** Unit cell of  $\text{Cu}_4\text{TiSe}_4$  placing Ti site at the centre of the unit cell. Ti, and Se atoms are represented by blue, and red coloured spheres, respectively. Four fold split copper sites (Cu2) around Cu3 (0,0,0) are shown. Cu1, Cu2 and Cu3 are represented in orange, light green and deep green color, respectively.

### Optical band gap determination using UV-Vis-NIR spectroscopy.

From the reflectance value, the Schuster–Kubelka–Munk function ( $F_{SKM}$ ) can be calculated[48] as:

$$F(R) = \frac{(1 - R)^2}{2R}$$

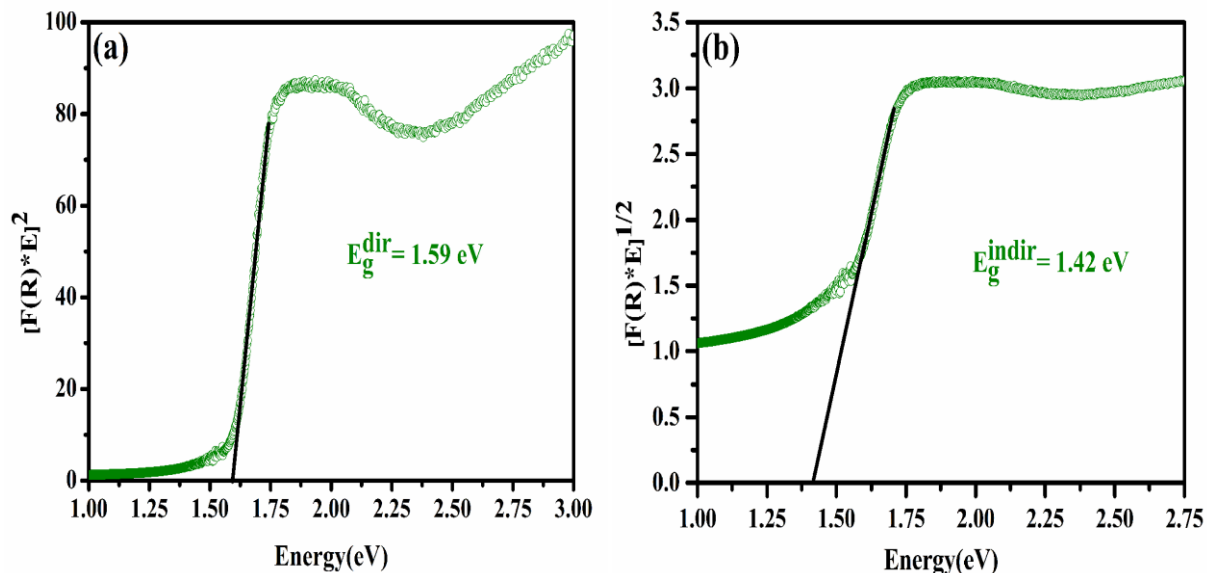
Where,  $R$ = reflectance (% of  $R/100$ ). Now, as  $F(R)$  is proportional to the optical absorption coefficient ( $\alpha$ ) [48], so Tauc equation [49] can be used for the analysis:

$$(\alpha h\nu)^{1/n} = A(h\nu - E_g)$$

The above equation can be written in terms of  $F(R)$  as:

$$[F(R)h\nu]^{1/n} = A(h\nu - E_g)$$

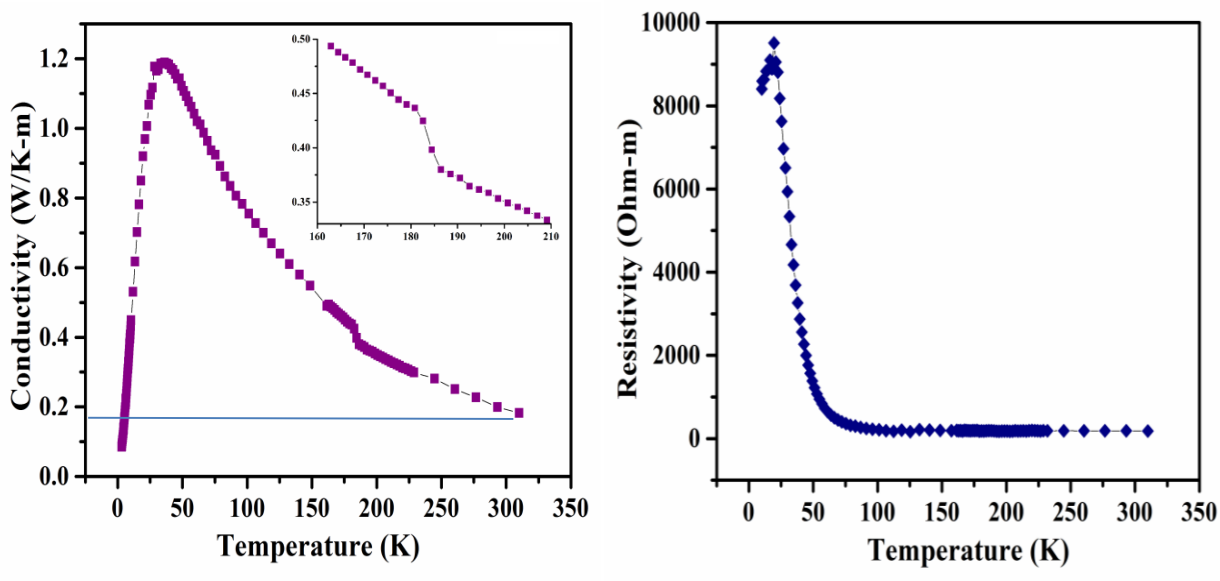
where,  $h$  is Planck's constant,  $\nu$  is the frequency of radiation,  $A$  is a constant,  $E_g$  is optical bandgap and the value of 'n' denotes the nature of the electronic transitions.  $n = 1/2$  corresponds to direct allowed transition (then  $E_g = E_g^{dir}$ = direct bandgap energy) and  $n=2$  corresponds to indirect allowed transition (then  $E_g = E_g^{indir}$ = indirect bandgap energy). From the extrapolation of  $(\alpha h\nu)^{1/n}$  versus  $h\nu$  curves to  $(\alpha h\nu)^{1/n} = 0$ , the value of  $E_g^{dir}$  and  $E_g^{indir}$  were determined 1.59 eV and 1.42 eV [Fig.3] respectively at 300 K temperature. Therefore, the compound is a wide bandgap semiconductor for room temperature applications. The optical band gap of this compound is comparable to the fundamental electronic band gap.



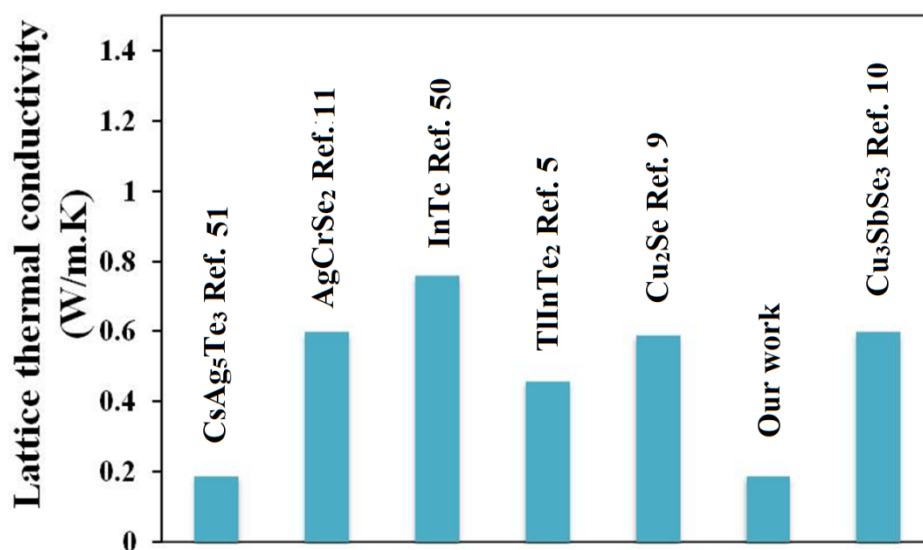
**Fig.3.** Tauc plots for optical band gap measurements showing **a)** direct bandgap and **b)** indirect bandgap of  $\text{Cu}_4\text{TiSe}_4$ .

### Thermal and electrical conductivity.

**Figure 4(left)** represents the temperature dependence of the thermal conductivity of  $\text{Cu}_4\text{TiSe}_4$ . At room temperature, total thermal conductivity ( $k_T$ ) was found to be extreme low ( $0.19 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ). The value at room temperature is much lower compared to the  $\text{Cu}_2\text{Se}$  [**Fig. 5**]. On moving to lower temperature the conductivity increases and there is a sudden increase in the value (from  $0.36 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  to  $0.43 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ ) at temperature 180K which is due to phase transformation. It is further confirmed by heat capacity measurement [**Fig. S5**].



**Fig.4** (left) Thermal conductivity vs temperature plot; (right) Resistivity vs temperature plot for phase pure  $\text{Cu}_4\text{TiSe}_4$  sample within the temperature range (4K to 310K).



**Fig.5.** Summary of the materials with ultra-low thermal conductivity at room temperature.

Thermal conductivity sharply increases with further lowering of temperature and reach to maxima at ~50K, then drop too steeply to 0.08 W·m<sup>-1</sup>·K<sup>-1</sup> at 4K [Fig. 4]. The measured electrical resistivity was used to extract electronic thermal conductivity ( $k_{el}$ ) with the help of the Wiedemann–Franz law. Thereafter,  $k_L$  is obtained from  $k_T$  by deducting  $k_{el}$  as  $k_T$  is combination of  $k_L$  and  $k_{el}$ . Since the compound is electrically insulating [Fig. 4] in nature, the measured thermal conductivity is  $k_L$ .

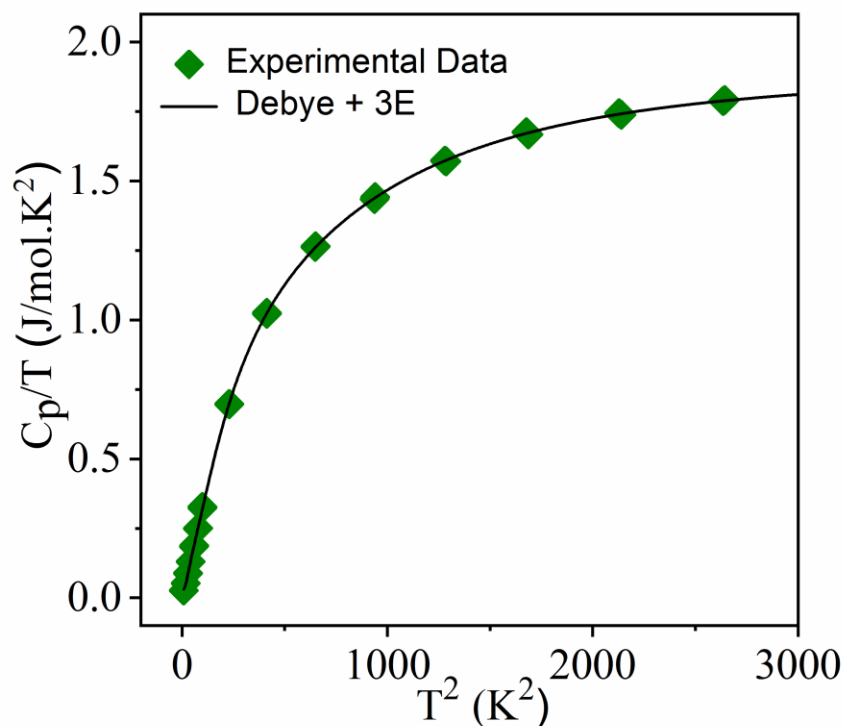
### Heat Capacity.

To get further insight, the heat capacity was measured between 2 and 300 K but data ranging from 2-55K was shown in the plot of  $C_p/T$  vs.  $T^2$  [Fig. 6]. The complete dataset ranging from 2-300K has been modelled using the combined Debye-Einstein model as following Eq:

$$\frac{C_p}{T} = \gamma + \beta T^2 + \sum_n \left( A_n (\Theta_{E_n})^2 \cdot (T^2)^{-3/2} \cdot \frac{e^{\Theta_{E_n}/T}}{(e^{\Theta_{E_n}/T} - 1)^2} \right)$$

In this equation, electronic contribution is introduced by  $\gamma$  and Debye mode contribution by  $\beta T^2$ , where  $\beta = C \cdot (12\pi^4 N_A k_B / 5) \cdot (\theta_D)^{-3}$  with  $N_A$ ,  $k_B$ ,  $\theta_D$  being the Avogadro number, Boltzmann constant and Debye temperature, respectively. The parameter C is given as  $C = 1 - \sum_n A_n / (3NR)$ , where N is the number of atoms per formula unit and R is the universal gas constant. The Debye temperature ( $\theta_D$ ) for the compound is estimated to be 204 K from the value of  $\beta$ . Three Einstein modes are estimated after modelling the temperature dependence through the fitting to whose characteristic temperatures to be 35.54K ( $\theta_{E1} = 24.7 \text{ cm}^{-1}$ ), 81.01K ( $\theta_{E2} = 56.3 \text{ cm}^{-1}$ ) and 179.24K ( $\theta_{E3} = 124.6 \text{ cm}^{-1}$ ; Table S4). The Einstein modes represent quasi-localized optical phonon modes arising from the vibrations of weakly bound atoms. Contribution to  $C_p$  at low temperatures is dominated by low-energy optical modes, which manifest as the Einstein oscillators. These low-

energy optical modes scatter the heat-carrying acoustic phonons thereby deteriorating the phonon transport of heat.



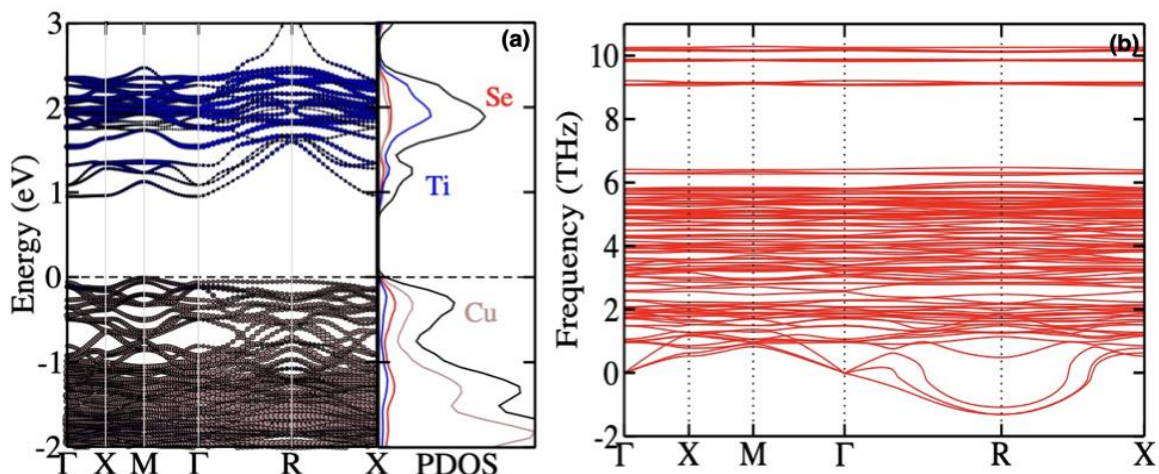
**Fig.6**  $C_p/T$  vs  $T^2$  plot.

### Electronic and phonon dispersion of the ordered supercell (SI2) from the disordered structure

The first principles density functional theory based calculations [Fig. 7] have been employed to calculate electronic structure of the supercell generated from disordered structure (SI2-a, Table S5, Fig. S6) using the GGA PBE XC functional. The electronic band structure of  $\text{Cu}_4\text{TiSe}_4$  is plotted along the high symmetry path  $\Gamma$ -X-M- $\Gamma$ -R-X in the irreducible part of the first Brillouin zone corresponding to the face-centered cubic lattice, which shows an indirect band gap ( $E_g = \sim 0.9$  eV), between the M (valence band maxima, VBM) and  $\Gamma$  (conduction band minima, CBm) point as shown in Fig. 7(a). The conduction bands and valence bands near the Fermi level are majorly

contributed by the Cu-d and Ti-d states as can be seen from the partial electronic contribution of the specific atoms in the density of states. The electronic band structure calculation is validated using the meta-GGA functional, which gave a similar trend of indirect band gap between the M (VBM) and  $\Gamma$  (CBM) point in the band structure. However, the magnitude band gap of 1.2 eV, is found to be  $\sim 25\%$  higher than the usually underestimated GGA band gap (see SI **Fig. S7**). In order to explore the effect of localized d electrons in the band gap, the calculations (GGA+U) were performed by incorporating the Hubbard U in the Hamiltonian (see SI, **Fig. S9**). The magnitude, the trend, and the elemental contributions in the CBM were found to be similar to the one calculated using meta GGA.

Except for the well known band gap estimation problem, no other noticeable change in bonding chemistry (viz. from the elemental contribution in VBM or CBM etc) was observed for the PBE GGA. Thus, PBE GGA was employed for performing the computationally demanding phonon calculations. The corresponding phonon band structure of the structure (of the converged 1X1X1 structure) is given in **Fig. 7(b)**. It shows the presence of imaginary acoustic phonon modes along the  $\Gamma$ -R-X direction of the dispersion, which in turn suggest towards dynamically unstable mode of vibrations. Thus, the presence of the instability in the structure prevents the use of Debye-Callaway or equivalent models for estimating the lattice thermal conductivity.



**Fig.7 a).** Electronic band dispersion and atom projected (coloured)/ total density of states (black), **b)** phonon band dispersion of the supercell (2x2x1) generated from the disordered  $\text{Cu}_4\text{TiSe}_4$  structure.

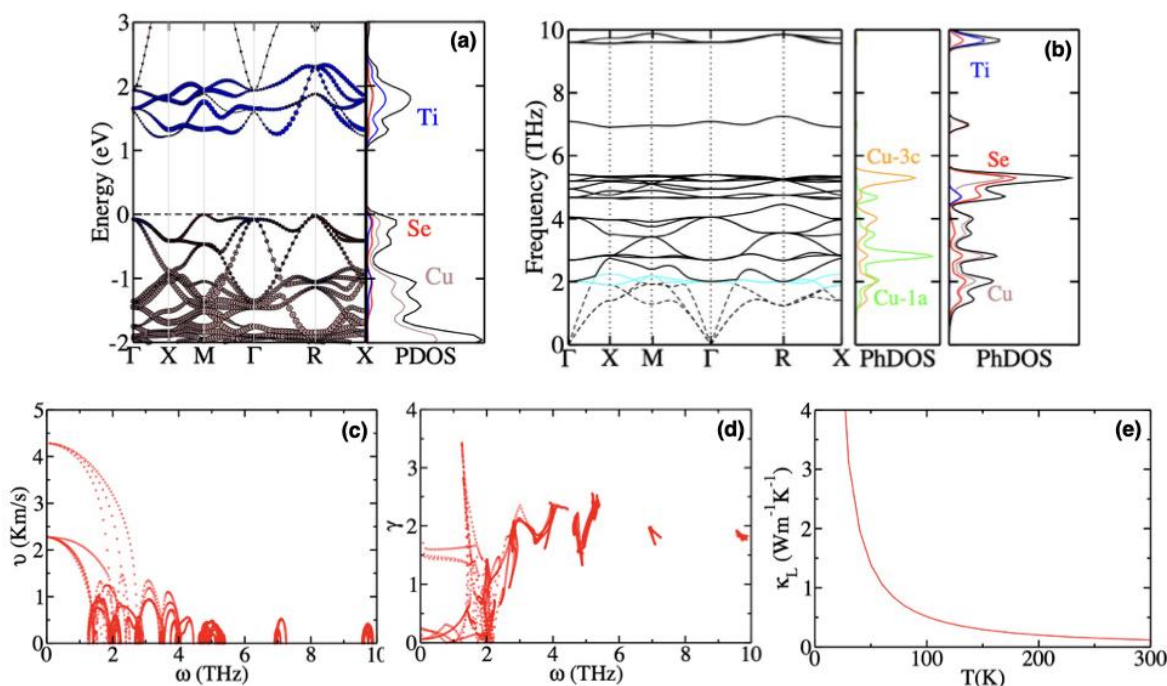
### Electronic and phonon dispersion of the ordered structure with original cell (1x1x1).

In order to get an idea of the lattice thermal conductivity a disorder free lattice is considered. The disorder free (SI2-b), structure of  $\text{Cu}_4\text{TiSe}_4$  comprises of nine atoms (with four Cu, four Se and one Ti) in one unit cell with a cubic structure with lattice parameter of 5.6 Å. This ground state configuration of  $\text{Cu}_4\text{TiSe}_4$  exists in the space group  $P\bar{4}3m$  with different ions occupying different Wyckoff positions viz. Cu [1a (0, 0, 0) and 3c (0.5, 0, 0.5)], Se [4e (0.23967, 0.23967, 0.23967)], and Ti [1b (0.5, 0.5, 0.5)]. The symmetry unique Cu-1a (green) and Cu-3c (orange) form the face-centered lattice, whereby half of the tetrahedral voids (alternate) are occupied by 4 Se atoms (red) and the center of the cube is occupied by a Ti atom (blue) [Fig. 2]. The electronic band structure of the ordered  $\text{Cu}_4\text{TiSe}_4$  show an indirect band gap of  $E_g = \sim 1.2$  eV as shown in Fig. 8(a). The corresponding discussion of the effect of the XC functional in the electronic band structure is provided as the supplementary information (see SI Fig.S8). The detailed phonon calculations are

performed on the stable ground state ordered structure. A convergence in the phonon density of states was reached for 2X2X2 supercell [see SI **Fig. S10**]. The converged phonon band structure and phonon partial density of states (PhDOSs) of the ordered  $\text{Cu}_4\text{TiSe}_4$  are shown in **Fig. 8(b)**, whereby the acoustic phonon modes are shown in dotted lines. It should be noted that the acoustic modes have low Debye cut off frequency (i.e. the frequency with which the modes reach the Brillouin zone boundary), since it is limited by the avoided crossing occurring due to the presence of the localized flat bands (shown in cyan) in the phonon band structure. As seen from the PhDOS presented in the middle panel of **Fig. 8(b)**, the localized modes of Cu-3c (orange) and Cu-1a (green) atoms equally contribute to the flat bands. However, these modes are not completely isolated ‘rattling’ modes, since they have slight dispersion or spread, which is due to the partial hybridization with Se-4e atom (as seen from the individual atomic contributions from phonon partial density of states). As seen from the last panel of **Fig. 8(b)**, the first peak due to the hybridization between the Cu-3c and Se-4e occurs at 1.4 THz ( $46.7 \text{ cm}^{-1}$ ), while a second peak is observed at 2.0 THz ( $66.72 \text{ cm}^{-1}$ ), which is due to the hybridization between the Cu-1a and Se-4e atoms. The mode resolved ( $v_i$ ) and average ( $v_s$ ) (calculated as  $\left[\frac{1}{3}\left(\frac{1}{v_{LA}^3} + \frac{1}{v_{TA}^3} + \frac{1}{v_{TA}^3}\right)\right]^{-\frac{1}{3}}$ ) phonon group velocity (Km/s), mode resolved Gruneisen parameter ( $\gamma_i$ ) and Debye temperature ( $\theta_D$ ) of the TA and LA branches as calculated from the phonon dispersion are enlisted in **Table 1** and shown in **Fig. 8(c)** and **(d)** respectively.  $v_i$  and  $\gamma_i$  are calculated from the average of group velocity and Gruneisen parameter attained by the modes originating from the  $\Gamma$  point in various direction of the Brillouin zone. Finally, the  $k_L$  is calculated by modelling the phonon scattering lifetime using the Debye Callaway formalism of solid. The temperature dependency of the lattice thermal conductivity computed for  $\text{Cu}_4\text{TiSe}_4$  is shown in **Fig. 8(e)**. As the temperature increases anharmonicity increases and therefore the lattice thermal conductivity decreases. At 300 K,  $k_L$  of

$\text{Cu}_4\text{TiSe}_4$  found to be  $0.12 \text{ W m}^{-1}\text{K}^{-1}$ , which is fairly in agreement to the experimental value. This ultralow value of  $\kappa_L$  can be attributed to the presence of the localized modes of Cu which was also partially dispersed due to their hybridization with the Se atoms. This, in turn leads to avoided crossing of acoustic phonon modes, which reach the zone boundary with a reduced frequency.

Although the  $\kappa_L$  of supercell model generated from the experimental disordered structure has not been calculated theoretically explicitly, but a close analogy can be drawn between the  $\kappa_L$  of the two structures. The acoustic phonon modes in the supercell model of the disordered structure reach the zone boundary at much lower frequency (by 40 %) than the corresponding ones in the ordered structure (which is the estimation of the Debye temperature,  $\theta_D$ ). Moreover, all the optical phonon modes in the supercell model ( $2 \times 2 \times 1$ ) of the disordered structure is composed majorly of flat bands, which implies zero group velocity (hence, no contribution to the  $\kappa_L$ ). Thus, low  $\theta_{DS}$  and flat optical phonon dispersion in the supercell model of the disordered structure suggests that the  $\kappa_L$  of the disordered structure will be even lower than the ordered structure which has been currently analyzed.



**Fig.8. a)** The electronic band structure of the ordered  $\text{Cu}_4\text{TiSe}_4$  (Cu (1a and 3c-brown), Se (4e-red) and Ti (1b-blue) atoms) with original cell, **b)** Phonon band structure (left panel) and partial density of states of the ordered  $\text{Cu}_4\text{TiSe}_4$  (right panel). Projected density of states of the symmetrically unique copper atoms, Cu-1a and Cu-3c (middle panel), **c)** The acoustic group velocity ( $v$ ), **d)** Grunesien parameter ( $\gamma$ ) plotted as a function of frequency ( $\omega$ ), and **e)** The lattice thermal conductivity  $k_L$  calculated using Debye Callaway formalism.

**Table 1.** The mode resolved ( $v_i$ ) and average ( $v_s$ ) phonon group velocity (Km/s), mode resolved Grunesien parameter ( $\gamma_i$ ) and Debye temperature ( $\theta_D$ ) of the TA and LA branches.  $k_L/300$  denotes the lattice thermal conductivity at 300 K.

System	$v_i$	$v_s$	$\gamma_i$	$\Theta_D k_L/300$
	$v_{TA} 1.9$		$\gamma_{TA} 6.0$	$\theta_{TA} 64$
$\text{Cu}_4\text{TiSe}_4$	$v_{TA}^* 1.9$	2.1	$\gamma_{TA}^* 6.0$	$\theta_{TA}^* 74$
	$v_{LA} 3.5$		$\gamma_{LA} 4.0$	$\theta_{LA} 86$

### Conclusion:

Recently discovered ternary copper titanium selenide  $\text{Cu}_4\text{TiSe}_4$  has been reinvestigated in this report. In contrast to previous report,  $\text{Cu}_4\text{TiSe}_4$  crystallizes centrosymmetric space group  $P\bar{4}3m$  ( $cP9$ ) and adopts  $\text{Cu}_3\text{VSe}_4$  structure ( $cP8$ ) type with an additional Cu site at (0 0 0). No evidence of superlattice is observed in the room temperature X-ray diffraction experiment. The room temperature structure displays positional disorder at copper sites, which is different finding from the previous report.  $\text{Cu}_4\text{TiSe}_4$  display high optical band gap of  $\sim 1.50$  eV. The compound shows

surprisingly high electrical resistivity in the order of  $10^2$  at room temperature. At room temperature, total thermal conductivity ( $k_T$ ) was found to be as low as  $0.19 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ . This major achievement results from strong optical-acoustic coupling with low cutoff frequencies and a rigid covalent bonding framework of Ti-Se interlocked with weakly bound ionic substructure comprising of  $\text{Cu}^+$  cations (intrinsic rattlers) which allows a thermal conductivity similar to that of a glass to be reached.  $\text{Cu}_4\text{TiSe}_4$  may have significant implications both in the field of thermal coating materials and solar cell absorber due to its nontoxicity and fabrication from the low cost earth abundant elements. Like phonon glass electron crystal,  $\text{Cu}_4\text{TiSe}_4$  with the ultra-low value of  $k_L$ , could also open the route for the discovery of efficient thermoelectric materials. Even, compound especially chalcogenides with relatively high electrical resistivity and large band gap deserve to be revisited, providing that their structures offer a sublattice with lightly bound cations.

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#### **Author contributions**

B.K. synthesized the samples, carried out structural characterization, model preparation for electronic structure calculation, performed data analysis, and wrote the maximum part of manuscript. A. L. synthesized the samples, performed DRS measurement and co-wrote the manuscript. P.R.R. and A.B. (IIT Bombay) performed calculations of electronic structure and phonon dispersion, wrote that section of manuscript. C. S. (NISER, Bhubaneswar) measured

thermal conductivity, electrical resistivity, heat capacity and helped to draw those pictures. P.P.J. conceived and supervised the entire project, performed crystal structure measurement, and structure determination helped to analyse the results and co-wrote the manuscript.

### Reference:

- [1] N. P. Padture, M. Gell, E. H. Jordan, *Science*, **2002**, 296, 280.
- [2] L. D. Zhao, V. P. Dravid, M. G. Kanatzidis, *Energy Environ. Sci.*, **2014**, 7, 251–268.
- [3] a) C. Chang, M. Wu, D. He, Y. Pei, C.-F. Wu, X. Wu, H. Yu, F. Zhu, K. Wang, Y. Chen, L. Huang, J.-F. Li, J. He, L. D. Zhao, *Science*, **2018**, 360, 778; b) L. D. Zhao, S. H. Lo, Y. Zhang, H. Sun, G. Tan, C. Uher, C. Wolverton, V. P. Dravid, M. G. Kanatzidis, *Nature*, **2014**, 508 (7496), 373–7; c) G. Tan, L. D. Zhao, F. Shi, J. W. Doak, S. H. Lo, H. Sun, C. Wolverton, V. P. Dravid, C. Uher, M. G. Kanatzidis, *J. Am. Chem. Soc.* **2014**, 136 (19), 7006–17; d) S. Roychowdhury, R. K. Biswas, M. Dutta, S. K. Pati, K. Biswas, *ACS Energy Lett.*, **2019**, 4, 1658.
- [4] a) M. Samanta, T. Ghosh, R. Arora, U. V. Waghmare, K. Biswas, *J. Am. Chem. Soc.*, **2019**, 141, 19505. b) M. K. Jana, K. Pal, A. Warankar, P. Mandal, U. V. Waghmare, K. Biswas, *J. Am. Chem. Soc.* **2017**, 139, 4350–4353.
- [5] S. Mukhopadhyay, D. S. Parker, B. C. Sales, A. A. Puretzky, M. A. McGuire, L. Lindsay, *Science*, **2018**, 360, 1455.
- [6] J. Yang, X. Wen, H. Xia, R. Sheng, Q. Ma, J. Kim, P. Tapping, T. Harada, T. W. Kee, F. Huang, Y. Cheng, M. Green, A. Ho-Baillie, S. Huang, S. Shrestha, R. Patterson, G. Conibeer *Nat. Comm.*, **2017**, 8 (1), 1-9.
- [7] T. Takabatake, K. Suekuni, T. Nakayama, E. Kaneshita, *Rev. Mod. Phys.* **2014**, 86, 669–716.
- [8] X. Shi, J. Yang, J. R. Salvador, M. Chi, J. Y. Cho, H. Wang, S. Bai, J. Yang, W. Zhang, L. Chen, *J. Am. Chem. Soc.* **2011**, 133, 7837–7846.
- [9] H. Liu, X. Shi, F. Xu, L. Zhang, W. Zhang, L. Chen, Q. Li, C. Uher, T. Day, G.J. Snyder, *Nat. Mater.* **2012**, 11, 422–425.
- [10] W. Qiu, L. Xi, P. Wei, X. Ke, J. Yang, W. Zhang, *Proc. Natl. Acad. Sci. U. S. A.* **2014**, 111, 15031.

- [11] B. Li, H. Wang, Y. Kawakita, Q. Zhang, M. Feyngenson, H. L. Yu, D. Wu, K. Ohara, T. Kikuchi, K. Shibata, T. Yamada, X. K. Ning, Y. Chen, J. Q. He, D. Vaknin, R. Q. Wu, K. Nakajima, M. G. Kanatzidis, *Nat. Mater.* **2018**, *17*, 226–230.
- [12] a) S. Ishiwata, Y. Shiomi, J. S. Lee, M. S. Bahramy, T. Suzuki, M. Uchida, R. Arita, Y. Taguchi, Y. Tokura, *Nat. Mater.*, **2013**, *12*, 512; b) S. Roychowdhury, M. K. Jana, J. Pan, S. N. Guin, D. Sanyal, U. V. Waghmare, K. Biswas, *Angew. Chem. Int. Ed.*, **2018**, *57*, 4043–4047.
- [13] X. Y. Shi, F.Q. Huang, M.L. Liu, L.D. Chen, *Appl.Phys.Lett.*, **2009**, *94*, 122103.
- [14] M. L. Liu, I.W. Chen, F.Q. Huang, L.D. Chen, *Adv. Mater.*, **2009**, *21*, 3808–3812.
- [15] X. Y. Shi, L. L. Xi, J. Fan, W.Q. Zhang, L.D. Chen, *Chem. Mater.* **2010**, *22*, 6029–6031.
- [16] J.Y. Cho, X. Shi, J.R. Salvador, G.P. Meisner, J. Yang, H. Wang, A.A. Wereszczak, X. Zhou, C. Uher, *Phys. Rev. B.*, **2011**, *84*, 085207.
- [17] E. J. Skoug, J. D. Cain, D. T. Morelli, *Appl. Phys. Lett.*, **2011**, *98*, 261911.
- [18] T. Plirdpring, K. Kurosaki, A. Kosuga, T. Day, S. Firdosy, V. Ravi, G. J. Snyder, A. Harneungmoung, T. Sugahara, Y. Ohishi, H. Muta, S. Yamanaka, *Adv. Mater.*, **2012**, *24*, 3622–3626.
- [19] R. Liu, L. Xi, H. Liu, X. Shi, W. Zhang, L. Chen, *Chem. Commun.*, **2012**, *48*, 3818–3820.
- [20] X. Lu, D. T. Morelli, Y. Xia, F. Zhou, V. Ozolins, H. Chi, X.Y. Zhou, C. Uher, *Adv. Energy Mater.*, **2013**, *3*, 342–348.
- [21] K. Suekuni, K. Tsuruta, M. Kunii, H. Nishiate, E. Nishibori, S. Maki, M. Ohta, A. Yamamoto, M. Koyano, *J. Appl. Phys.*, **2013**, *113*, 043712.
- [22] Y. Goto, Y. Kamihara, M. Matoba, *J. Electron Mater.*, **2014**, *43*, 2202–2205.
- [23] A. Suzumura, N. Nagasako, Y. Kinoshita, M. Watanabe, T. Kita, R. Asahi, *Mater. Trans.*, **2015**, *56*, 858–863.
- [24] J. Fan, W. Carrillo-Cabrera, L. Akselrud, I. Antonyshyn, L. Chen, Y. Grin, *Inorg. Chem.*, **2013**, *52*, 11067–11074.

[25] a) Q. Guo, G. M. Ford, W. C. Yang, B. C. Walker, E. A. Stach, H. W. Hillhouse, R. Agrawal, *J. Am. Chem. Soc.*, **2010**, *132*, 17384–17386; b) S. C. Riha, B. A. Parkinson, A. L. Prieto, *J. Am. Chem. Soc.*, **2009**, *131*, 12054–12055; c) S. C. Riha, B. A. Parkinson, A. L. Prieto, *J. Am. Chem. Soc.*, **2011**, *133*, 15272–15275.

[26] a) D. B. Mitzi, O. Gunawan, T. K. Todorov, K. Wang, S. Guha, *Energy Mater. Sol. Cells*, **2011**, *95*, 1421–1436. b) E. Osei-Agyemang, G. Balasubramanian, *ACS App. Energy Mater.* **2020**, *1*, 1139–1144. c) E. Osei-Agyemang, C. E. Adu, G. Balasubramanian, *Adv. Theo. Simu.* **2019**, *2*, 1900060.

[27] Q. Guo, H. W. Hillhouse, R. Agrawal, *J. Am. Chem. Soc.*, **2011**, *131*, 11672–11673.

[28] C. Steinhagen, M. G. Panthani, V. Akhavan, B. Goodfellow, B. Koo, B. A. Korgel, *J. Am. Chem. Soc.*, **2011**, *131*, 12554–12555.

[29] a) M. G. Panthani, V. Akhavan, B. Goodfellow, J. P. Schmidtke, L. Dunn, A. Dodabalapur, P. F. Barbara, B. A. Korgel, *J. Am. Chem. Soc.*, **2008**, *130*, 16770–16777; b) P. Jackson, D. Hariskos, E. Lotter, S. Paetel, R. Wuerz, R. Menner, W. Wischmann, M. Powalla, *Photovolt.: Res. Appl.*, **2011**, *19*, 894–897; c) J. Y. Kim, J. Yang, J. H. Yu, W. Baek, C.-Ho Lee, H. J. Son, T. Hyeon, M. J. Ko, *ACS Nano*, **2015**, *9*(11), 11286–11295.

[30] K. O. Klepp, D. Gurtner, *J. Alloys and Compd.*, **1996**, *243*, 19–22.

[31] P. M. Keane, J. A. Ibers, *J. Solid State Chem.*, **1991**, *93*, 291–297.

[32] E. M. Chen, L. Williams, A. Olvera, C. Zhang, M. Zhang, G. Shi, J. T. Heron, L. Qi, L. J. Guo, E. Kioupakis, P. F. P. Poudeu, *Chem. Sci.*, **2018**, *9*, 5405–5414.

[33] L. Pauling, R. Hultgren, *Z. Kristallogr.*, **1932**, *84*, 204.

[34] K. O. Klepp, D. Gurtner, *Z. Kristallogr.*, **2000**, *215*, 4.

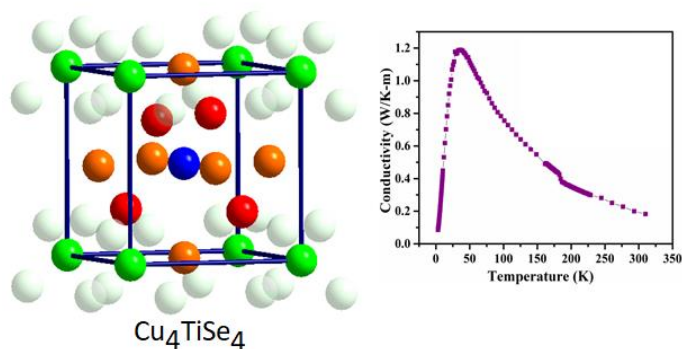
[35] G. E. Delgado, A. J. Mora, S. Durán, M. Muñoz, P. G. Gallardo, *J. Alloys and Compd.*, **2007**, *439*, 346–349.

[36] Y. J. Lu, J. A. Ibers, *Journal of Solid State Chemistry*, **1993**, *107*, 58–62.

- [37] G. E. Delgado, A. J. Mora, P. G. Gallardo, S. Durán, M. Muñoz, M. Quintero, *Chalcogenide Letters*, **2009**, *69*, 335 – 338.
- [38] A. B. Kehoe, D. O. Scanlon and G. W. Watson, *J.Mater. Chem. C*, **2015**, *3*, 12236-12244.
- [39] L. Palatinus, G. Chapuis, *Journal of Applied Crystallography*, **2007**, *40*, 786-790.
- [40] V. Petříček, M. Dušek, L. Palatinus, The crystallographic computing system, Institute of Physics, *Academy of Sciences of the Czech Republic*, **2006**, *162*, 53.
- [41] P. Hohenberg, W. Kohn, *Phys.Rev.*, **1964**, *136*, 864–871.
- [42] W. Kohn, L. J. Sham, *Phys. Rev.*, **1965**, *140*, 1133–1138.
- [43] G. Kresse, J. Hafner, *Phys.Rev.B.*, **1994**, *49*, 14251–14269.
- [44] J. P. Perdew, K. Burke, M. Ernzerhof, *Phys.Rev.Lett.*, **1996**, *77*, 3865–3868.
- [45] A. Togo and, I. Tanaka, *Scr.Mater.*, **2015**, *108*, 1-5.
- [46] (a) A. Bhattacharya, *Journal of Materials Chemistry C*, **2019**, *7*, 13986-13992. (b) A. Bhattacharya, *Journal of Physics: Condensed Matter*, **2020**, *32*, 175502.
- [47] (a) X. Chen, M. Onoda, H. Wada, A. Sato, H. Herbst-Irmer, *Journal of Solid State Chemistry*, **1999**, *145*, 204 -211. (b) A. Choudhury *et al.* New insights into the structure, chemistry, and properties of Cu<sub>4</sub>SnS<sub>4</sub>. *Journal of Solid State Chemistry*, **2017**, *253*, 192–201.
- [48] M. Patel, A. Chavda, I. Mukhopadhyay, J. Kimband, A. Ray, *Nanoscale*, **2016**, *8*, 2293–2303.
- [49] J. Tauc, R. Grigorovici and A. Vancu, *Physica Status Solidi*, **1966**, *15*, 627-637.
- [50] M. K. Jana, K. Pal, U. V. Waghmare, K. Biswas, *Angew. Chem. Int. Ed.*, **2016**, *55*, 7792–7796.
- [51] H. Lin *et al.* *Angew. Chem. Int. Ed.*, **2016**, *55*, 11431–11436.

Keywords: X-ray diffraction, atomic disorder, ultra-low thermal conductivity, phonon dispersion, electronic band structure.

Table of Contents:



$\text{Cu}_4\text{TiSe}_4$  is a unique example of a non-toxic and low-cost material that exhibits lattice ultra-low thermal conductivity of  $0.19 \text{ W m}^{-1}\text{K}^{-1}$  at room temperature. The main contribution to the unusually low thermal conductivity is connected with the atomic lattice and its dynamics.